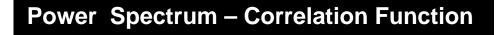
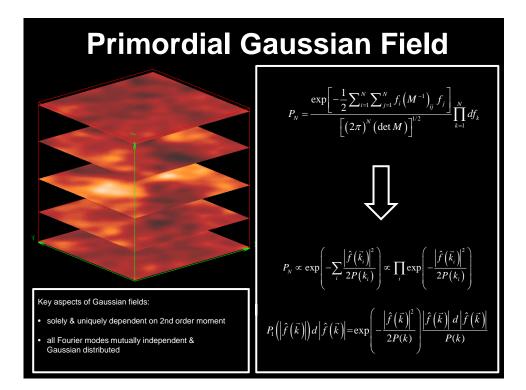


Power Spectrum P(k) specifies the relative contribution of different scales to the density fluctuation field. It entails a wealth of cosmological information. $\sigma^{2} = \int \frac{d\vec{k}}{(2\pi)^{3}} P(k) \qquad \Leftrightarrow \qquad P(k) \propto \left\langle \hat{f}(\vec{k}) \hat{f}^{*}(\vec{k}) \right\rangle$ Formal definition: $\left(2\pi\right)^{3} P(k_{1}) \ \delta_{D}\left(\vec{k}_{1} - \vec{k}_{2}\right) = \left\langle \hat{f}\left(\vec{k}_{1}\right) \hat{f}^{*}\left(\vec{k}_{2}\right) \right\rangle$ \downarrow $P(k) \propto \left\langle \hat{f}\left(\vec{k}_{1}\right) \hat{f}^{*}\left(\vec{k}_{2}\right) \right\rangle$



Gaussian random field fully described by 2nd order moment:

- in Fourier space: - in Configuration (spatial) space: 2-pt correlation function $(2\pi)^{3} P(k_{1}) \delta_{D}(\vec{k}_{1} - \vec{k}_{2}) = \langle \hat{f}(\vec{k}_{1}) \hat{f}^{*}(\vec{k}_{2}) \rangle$ $P(k) = \int d^{3}r \ \xi(\vec{r}) \ e^{i\vec{k}\cdot\vec{r}}$ $\xi(\vec{r}_{1}, \vec{r}_{2}) = \xi(|\vec{r}_{1} - \vec{r}_{2}|) = \langle f(\vec{r}_{1}) f(\vec{r}_{2}) \rangle$ $\zeta(\vec{r}) = \int \frac{d^{3}k}{(2\pi)^{3}} P(k) \ e^{-i\vec{k}\cdot\vec{r}}$



Power Spectrum

P(k) specifies the relative contribution of different scales to the density fluctuation field. It entails a wealth of cosmological information.

$$\sigma^{2} = \int \frac{dk}{\left(2\pi\right)^{3}} P(k) \qquad \Leftrightarrow \qquad P(k) \propto \left\langle \hat{f}(\vec{k}) \hat{f}^{*}\left(\vec{k}\right) \right\rangle$$

Power Law Power Spectrum:

$$P(k) \propto k^n$$

as index n lower, density field increasingly dominated by large scale modes. For an arbitrary spectrum,

$$n(k) = \frac{d\log P(k)}{d\log k}$$

